Block:

Seat:

Chapter 2B skills Check List:

1 Related Rates Word Problems (Section 2.6).

Chapter 3 skills Check List:

1 Absolute (p166) and Relative Extrema (p167) 3 Practice MVT (3 skills)

2 Critical Numbers (168)

3 Extreme Value Theorem (EVT) (p166)

4 Candidates Test (p 169)

5 Rolle's Theorem (p 174)

6 Mean Value Theorem (MVT) for rates (p 176)

Increasing and Decreasing (181)

8 1^{st} Derivative Test for Relative Extrema (p 183)

9 Concavity (p. 192-193)

10 Points of Inflection (POI) (p.193-194)

11 2^{nd} Derivative Test for Relative Extrema (p 195)

12 Limits at $\pm \infty$ (end behavior) (p 199-200, 205)

13 Horizontal Asymptote (p. 200)

14 Curve Sketching (Section 3.6)

15 Optimization Word Problems (Section 3.7)

Delta Math Check List:

Name:

1 Practice Related Rates (4 skills)

2 Practice EVT (2 skills)

4 Practice Function Analysis (3.3) (6 skills)

5 Practice Function Analysis (3.4) (6 skills)

Khan Academy Check List:

1 Contextual applications of Derivatives Unit topic: Solving Related Related Rates Problems (AP Unit 4.4)

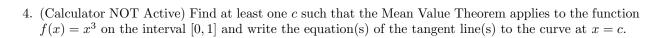
2 Applying Derivatives to Analyze Functions Unit (AP Unit 5)

1. Use the Candidates Test to identify the absolute extrema of $f(x)=x^3-6x^2+9x+5$ on the interval $0\leq x\leq 4$.

2. Use the Candidates Test to identify the absolute extrema of $f(x) = x + \frac{7}{x}$ on the interval $1 \le x \le 3$.

3. Let f be a twice differentiable function. If f'(7) = 0 and f''(7) > 0 what conclusion can be made and why?

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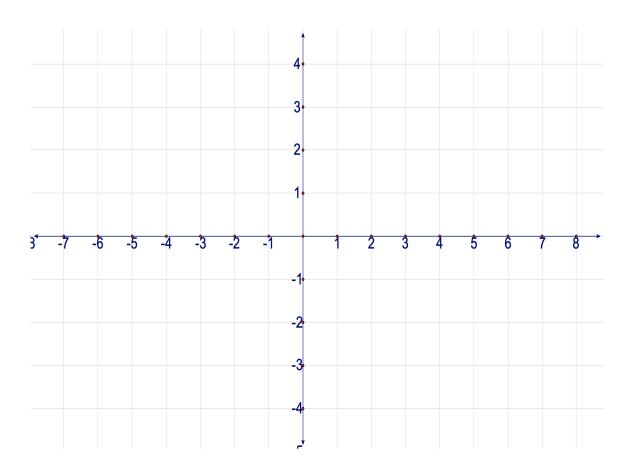
5. (Calculator Active) Find all c on [0,2] such that the Mean Value Theorem applies to the function $f(x) = x^2 + 3x - 4\sin(2x + 3)$ on the interval [0,2].

6. Find absolute extrema for the function $f(x) = x^3 - 3x + 2$ on the interval [-3, 2]. Justify your conclusion.

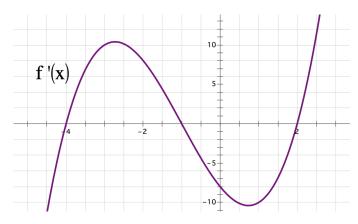
- 7. Let $f(x) = x^3 3x + 2$.
 - (a) Find f' and f'',
 - (b) Find the critical points of f' and f''.
 - (c) Draw sign lines for f' and f''
 - (d) On what intervals are f increasing and decreasing? Justify.
 - (e) On what intervals are f concave up or down? Justify.
 - (f) Find all relative extrema and justify your conclusions with the 1^{st} Derivative Test
 - (g) Find all relative extrema and justify your conclusions with the 2^{nd} Derivative Test
 - (h) If any exist, find any points of inflection (POI). Justify.
 - (i) What is the end behavior of f (That is, find $\lim_{x\to\pm\infty}f(x))$

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- 8. (Calculator NOT active) Given the function $g(x) = \frac{4x}{x^2 + 1}$, its 1^{st} derivative $g'(x) = \frac{4(1 x^2)}{(x^2 + 1)^2}$ and its 2^{nd} derivative $g''(x) = \frac{8x(x^2 3)}{(x^2 + 1)^3}$
 - (a) Make sign lines for g, g', and g''
 - (b) Find the (x, y) coordinates of any intercepts, and graph them.
 - (c) Find any vertical or horizontal asymptotes and g's end behavior (i.e.: $\lim_{x\to\pm\infty}g(x)$) and use this to improve the graph.
 - (d) Find the relative extrema and indicate them on the graph with a small horizontal bar through any extrema.
 - (e) Improve the graph by noting where it is concave up or concave down, and find any points of inflection. Indicate a POI on the graph with a small perpendicular bar through the point.

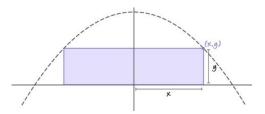


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- 9. (Calculator NOT active) Given the graph of f'(x) above:
 - (a) Approximate the sign lines for f'(x) and f''(x).
 - (b) Find a relative maximum of f and use the $\mathbf{1}^{st}$ Derivative Test to justify your conclusion.
 - (c) Find a relative minimum of f and use the 2^{nd} Derivative Test to justify your conclusion.
 - (d) On what interval(s) is f increasing? Justify.
 - (e) On what interval(s) is f decreasing? Justify.
 - (f) On what interval(s) is f concave up? Justify.
 - (g) On what interval(s) is f concave down? Justify.
 - (h) Find all the points of inflection of f, and justify why it is a point of inflection.

10. (Calculator NOT Active) A rectangle has its bottom edge on the x axis and its top corners are on the the graph $y=6-\frac{x^2}{24}$ What length and width should the rectangle have so that the rectangle has the largest area?



11. (Calculator NOT Active) Engineers are designing a box-shaped aquarium with a square bottom and an open top. The aquarium must hold 500 cubic feet of water. What dimensions should they use to create an acceptable aquarium with the least amount of glass?



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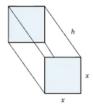
12. In 1977 P.M. Tuchinsky wrote an article called "The Human Cough". In it, the speed s of the air leaving your windpipe as you cough can be modeled by the function

$$s(x) = kx^2(R - x)$$

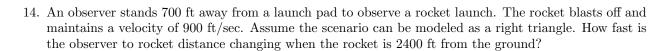
where R is radius of your windpipe (trachea) while resting (a positive constant), x is the radius of your windpipe while coughing (a positive variable), and k is positive constant.

If for a particular person $k = \frac{1}{3}$ and R = 27 mm, find the absolute maximum speed on the interval $0 \le x \le 27$. (Your answer will be in terms of mm per second)

13. A box has 2 square ends and 4 rectangular sides. The square ends are made out of plastic that costs \$5 dollars per square foot, and the cardboard sides cost \$3 dollars per square foot. Find the dimensions of the box that has a volume of 60 cubic feet, that is the cheapest to make. *Hint*: Use the candidates test, first derivative test, or second derivative test to justify your claim that it is indeed the minimum cost.



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15. A conical paper cup is 10 cm tall with a radius of 10 cm. The cup is being filled with water so that the water level rises at a rate of 2 cm/sec. At what rate is the volume of water growing at the moment when the water level is 8 cm?. The volume of a cone is given by $V = \frac{\pi}{3}r^2 \cdot h$